InfO(1) Cup, Day 2
Ploiești, Romania
Sunday $11^{\text {th }}$ February, 2024

## Problem Lattice

| Input file | stdin |
| :--- | :--- |
| Output file | stdout |

For every two positive integers $N, M$, we define lattice $(N, M)$ to be those points $(x, y)$ for which $N$ divides $x$ and $M$ divides $y$, and where $x, y$ are non-negative integers. In other words, the points of lattice $(N, M)$ can be thought of as those points reachable from $(0,0)$ by moving a multiple of $N$ steps to the right, and a multiple of $M$ steps up. For example, lattice $(2,3)$ looks like this.


Given $K$ and a list of $P$ points $\left(x_{1}, y_{1}\right), \ldots,\left(x_{P}, y_{P}\right)$ with integer coordinates in the plane, answer the following question: For how many positive integers $x$ does lattice $(x, x)$ contain at least $K$ of the $P$ points?

## Input data

The first line of the input contains $P$ and $K$. The next $P$ lines contain the points $\left(x_{i}, y_{i}\right)$.

## Output data

The first line of the output should contain the answer to the question.

## Restrictions

- $1 \leq x_{i}, y_{i} \leq 1000000$
- $1 \leq K \leq P \leq 200000$

| $\#$ | Points | Restrictions |
| :--- | :---: | :--- |
| 1 | 16 | All the values from input are at most 1000 |
| 2 | 11 | All the values from input are at most 100000 |
| 3 | 15 | $x_{i}=y_{i}$ for all the points |
| 4 | 21 | The sequence $x_{1}, \ldots, x_{P}, y_{1}, \ldots, y_{P}$ contains pairwise distinct elements. |
| 5 | 37 | No further restrictions. |

## Examples

|  | Input file | Output file |
| :--- | :--- | :--- |
| 3 | 2 | 1 |
| 1 | 3 |  |
| 3 | 6 |  |
| 4 | 2 |  |
| 5 | 2 | 3 |
| 2 | 2 |  |
| 5 | 10 | 4 |
| 15 | 5 |  |
| 17 | 7 |  |

## Explanations

First example. In the first example, only lattice $(1,1)$ contains at least 2 points.

Second example. Here, lattice $(1,1)$ contains all the points, lattice $(2,2)$ has the first and the third point and lattice $(5,5)$ has the second and the fourth point. Below is a grid showing all the lattices. lattice $(1,1)$ is the underlying grid, lattice $(2,2)$ is marked by red $x$ 's, and lattice $(5,5)$ is marked by blue x's. The points in all three lattices are marked by purple x's. The $P$ points in the input are marked by filled-in circles $(\cdot)$, with the colour showing which grid they belong to: if a point is only in lattice $(1,1)$ it is gray, if it is in lattice $(1,1)$ and lattice $(2,2)$ it is red, and if it is in lattice $(1,1)$ and lattice $(5,5)$ it is blue.


